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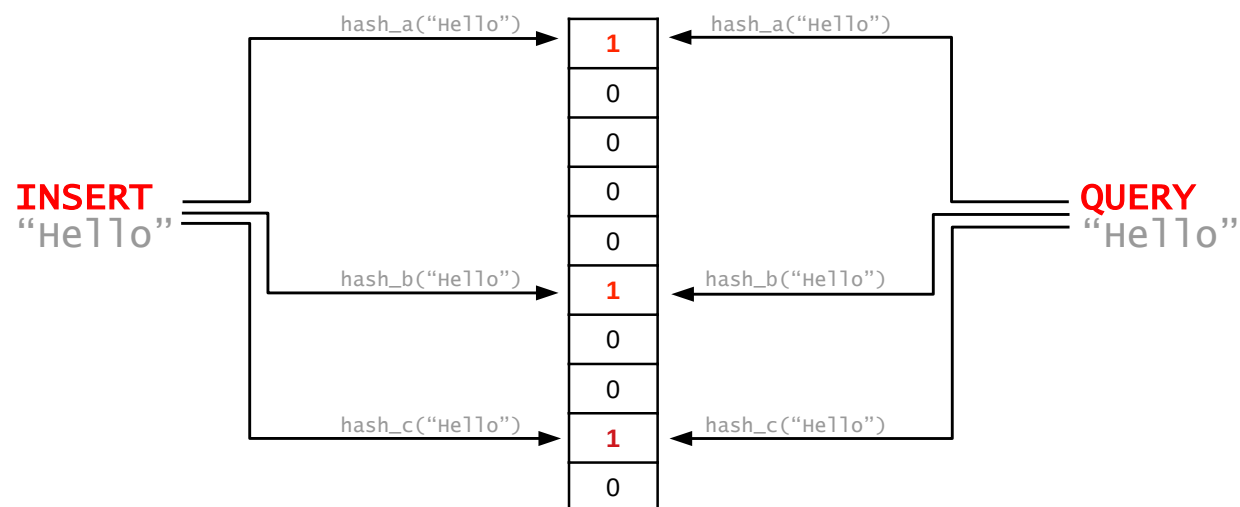
ETH Zürich
Oct. 11 2018

Last week on
Advanced Topics in Communication Networks

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Probabilistic data structures like Bloom Filters
help to trade resources with accuracy

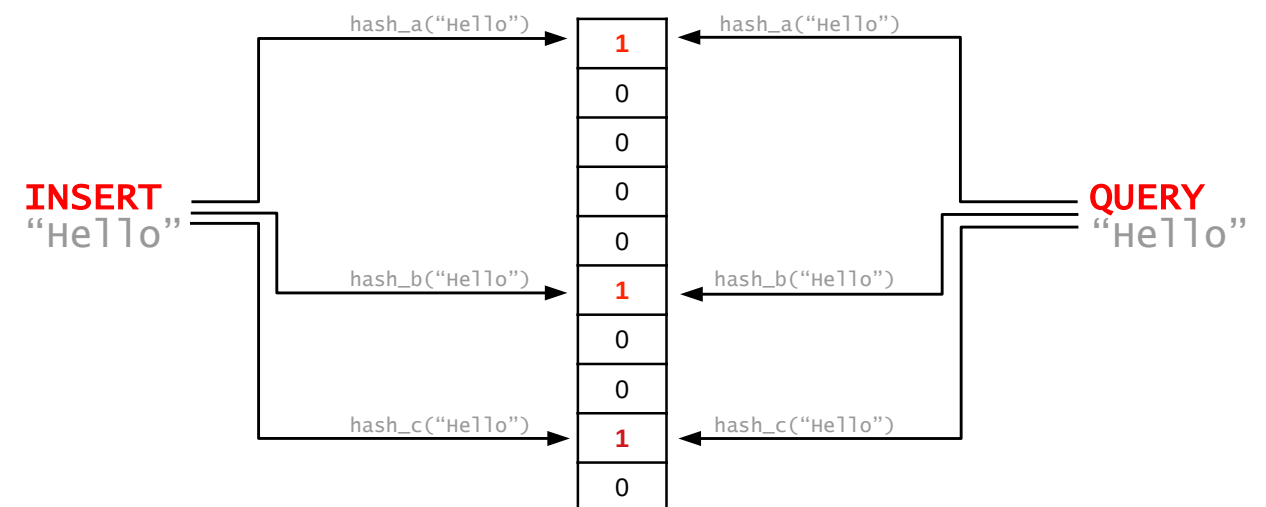
Recap



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Bloom Filters take a fixed number of operations,
but hash collisions can cause false positives.

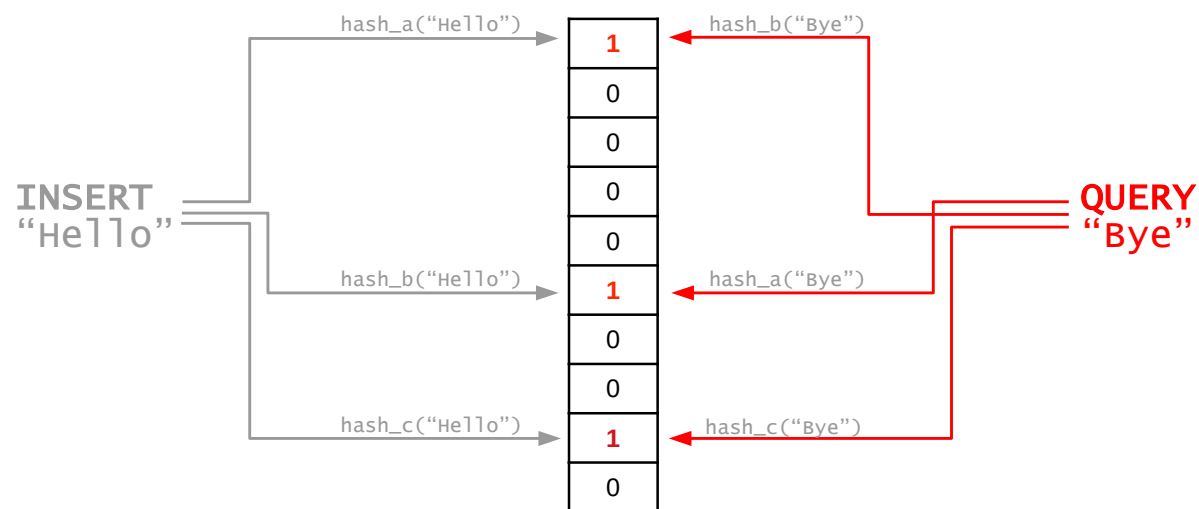
Recap



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Bloom Filters take a fixed number of operations,
but hash collisions can cause **false positives**

Recap



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Recap

A bloom filter is a streaming algorithm
answering specific questions approximately.

Is X in the stream?
What is in the stream?

Invertible Bloom Filter

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Recap

A bloom filter is a streaming algorithm
answering specific questions approximately.

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A bloom filter is a streaming algorithm
answering specific questions approximately.

Is X in the stream?
What is in the stream?

Invertible Bloom Filter

What about other questions?

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Today we'll talk about: **important questions,**

how 'sketches' answer them,

and limitations of 'sketches'

my master thesis :)

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*In networking, we talk about **flows of packets**,
but these questions apply to other domains as well,
e.g. **search engines and databases**.*

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Is a certain flow in the stream?

Bloom Filter

What flows are in the stream?

Invertible Bloom Filter, HyperLogLog Sketch, ...

How frequent does an flow appear?

Count Sketch, CountMin Sketch, ...

What are the most frequent elements?

Count/CountMin + Heap, ...

How many flows belong to a certain subnet?

SketchLearn SigComm '18

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Bloom Filter

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Count/CountMin + Heap, ...

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SketchLearn SIGCOMM '18

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We are going to look at **frequencies**,
i.e. **how often** an element occurs in a data stream.

$$\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \end{bmatrix}$$

vector of frequencies (counts)
of all **distinct elements** x_i

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In the worst case, an algorithm providing
exact frequencies requires **linear space**.

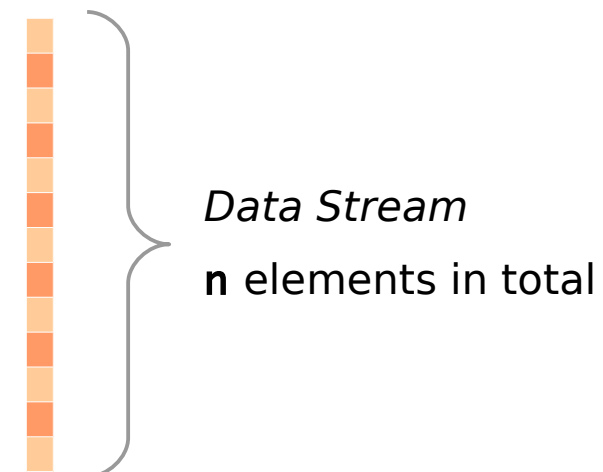
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vector of frequencies (counts)
of all **distinct elements** x_i
distinct flows

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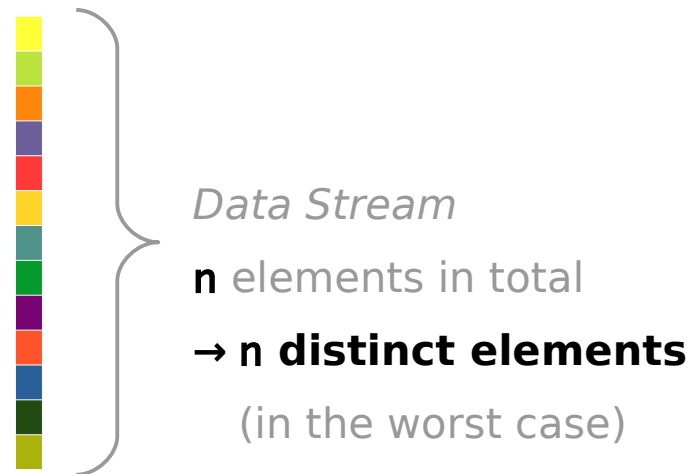
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15

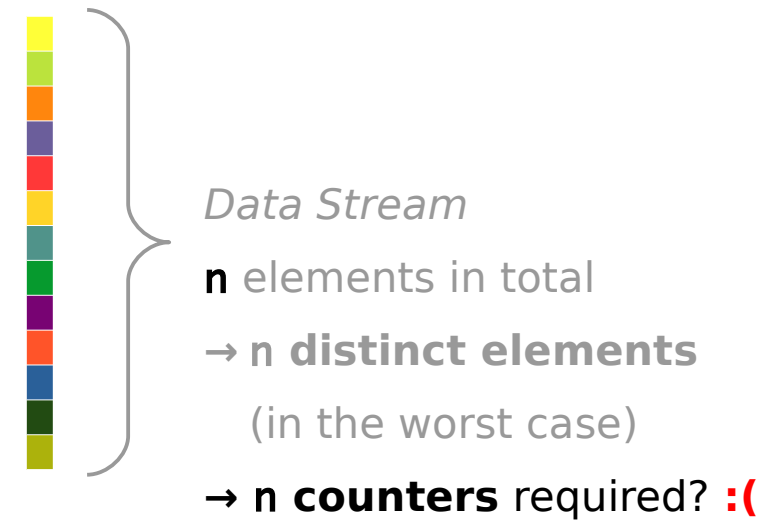
16

In the worst case, an algorithm providing **exact frequencies** requires **linear space**.



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In the worst case, an algorithm providing **exact frequencies** requires **linear space**.



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Probabilistic datastructures can help again!

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Bloom Filters

quickly “filter” only those elements that might be in the set

Save space by allowing false positives.

Bloom Filters

quickly “filter” only those elements that might be in the set

Save space by allowing false positives.

Sketches

provide a approximate frequencies of elements in a data stream.

Save space by allowing mis-counting.

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Today we'll talk about: important questions,
how 'sketches' answer them,
limitations of 'sketches',
and my master thesis :)

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A **CountMin sketch** uses the same principles as a counting bloom filter, but is **designed** to have **provable L1 error bounds** for frequency queries.

Notation reminder:
vector of frequencies (counts)
of all **distinct elements** x_i

$$\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \end{bmatrix}$$

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A **CountMin sketch** uses the same principles as a counting bloom filter, but is **designed** to have **provable L1 error bounds** for frequency queries.

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A **CountMin sketch** uses the same principles as a counting bloom filter, but is **designed** to have **provable L1 error bounds** for frequency queries.

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$$Pr \left[\underbrace{\hat{x}_i}_{\text{estimated frequency}} - \underbrace{x_i}_{\text{true frequency}} \geq \epsilon \underbrace{\|\mathbf{x}\|_1}_{\text{sum of frequencies}} \right] \leq \delta$$

The estimation error **exceeds** $\epsilon \|\mathbf{x}\|_1$
with a **probability smaller than** δ

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$$Pr \left[\underbrace{\hat{x}_i}_{\text{estimated frequency}} - \underbrace{x_i}_{\text{true frequency}} \geq \epsilon \underbrace{\|\mathbf{x}\|_1}_{\text{sum of frequencies}} \right] \leq \delta$$

relative to L1 norm

The estimation error **exceeds** $\epsilon \|\mathbf{x}\|_1$
with a **probability smaller than** δ

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$$Pr \left[\underbrace{\hat{x}_i}_{\text{estimated frequency}} - \underbrace{x_i}_{\text{true frequency}} \geq \epsilon \underbrace{\|\mathbf{x}\|_1}_{\text{sum of frequencies}} \right] \leq \delta$$

Let $\epsilon = 0.01$, $\delta = 0.05$, $\|\mathbf{x}\|_1 = 10000$

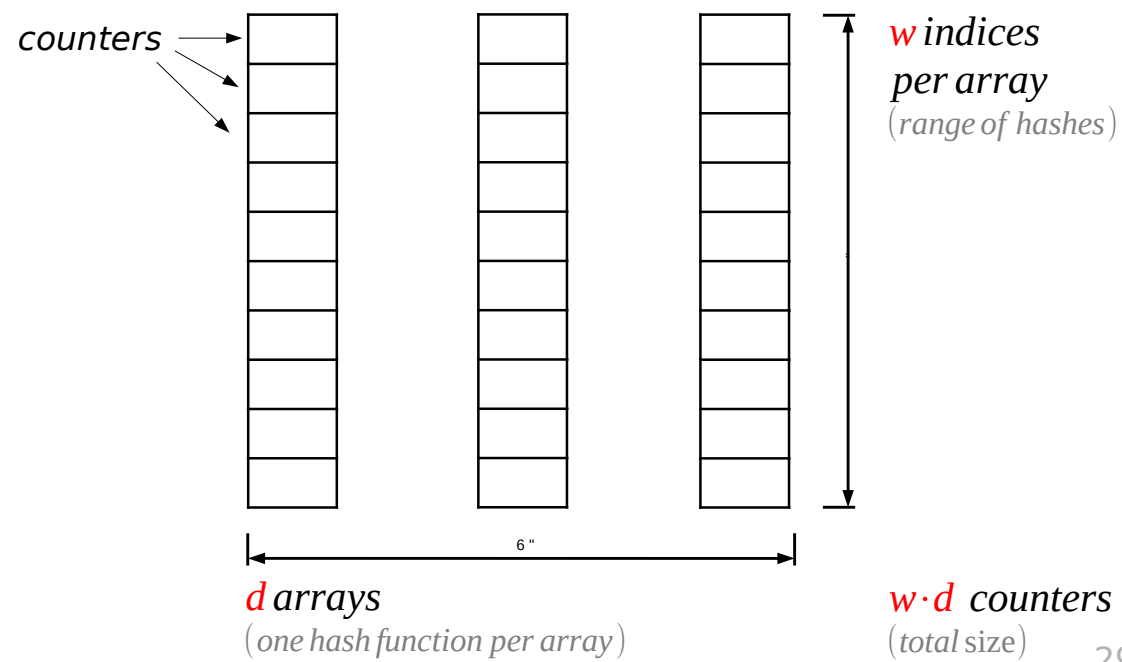
The probability for **any estimate** to be
off by **more than 100** is **less than 5%**
(after counting 10000 elements)

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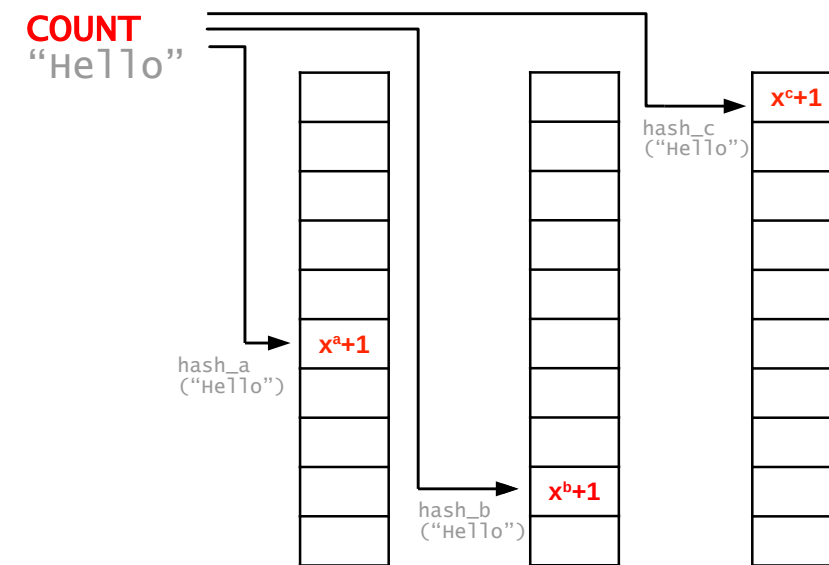
A **CountMin sketch** uses the same principles as a counting bloom filter, but is **designed** to have **provable L1 error bounds** for frequency queries.

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A **CountMin** Sketch uses multiple arrays and hashes.

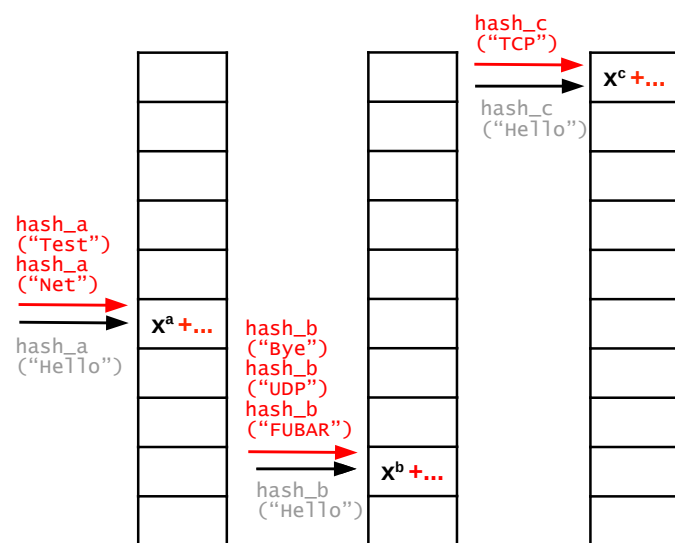


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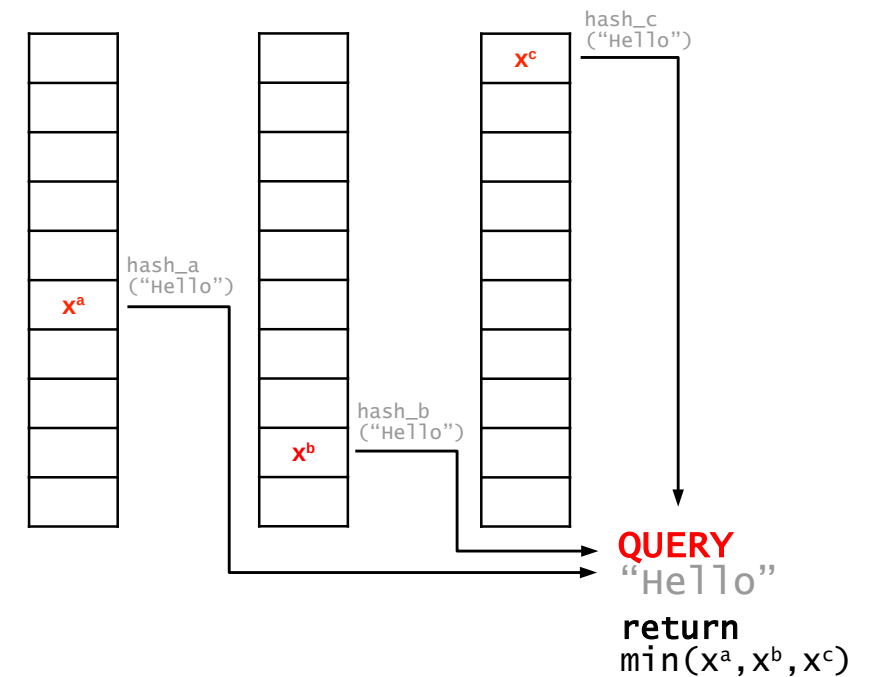
30

Hash collisions cause **over-counting**.



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Returning the **minimum value** minimizes the error.



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A **CountMin sketch** uses the same principles as a counting bloom filter, but is designed to have **provable L1 error bounds** for frequency queries.

$$Pr \left[\underbrace{\hat{x}_i}_{\text{estimated frequency}} - \underbrace{x_i}_{\text{true frequency}} \geq \underbrace{\varepsilon \|\mathbf{x}\|_1}_{\text{sum of frequencies}} \right] \leq \delta$$

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Understanding the error bounds allows **dimensioning** the sketch optimally.

Error Bounds
per hash/array

Error Bounds
for the minimum

Optimal Size

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Error Bounds
per hash/array

$$\underbrace{\hat{x}_i}_{\text{estimated frequency}} = \min_{h \in h_1 \dots h_d} \underbrace{\hat{x}_i^h}_{\text{estimate for specific hash}}$$

Error Bounds
per hash/array

$$\underbrace{\hat{x}_i}_{\text{estimated frequency}} = \min_{h \in h_1 \dots h_d} \underbrace{\hat{x}_i^h}_{\text{estimate for specific hash}}$$

Error Bounds
for the minimum

Optimal Size

Error Bounds
for the minimum

Optimal Size

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The error bounds can be derived
with **Markov's Inequality**

Error Bounds
per hash/array

$$\Pr [X \geq c \cdot E[X]] \leq \frac{1}{c}$$

Error Bounds
for the minimum

Optimal Size

wikipedia.org/wiki/Markov's_inequality 37

The error bounds can be derived
with **Markov's Inequality**

Error Bounds
per hash/array

$$\Pr [\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

Error Bounds
for the minimum

Optimal Size

wikipedia.org/wiki/Markov's_inequality 38

Error Bounds
per hash/array

$$\Pr [\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

Error Bounds
for the minimum

$$\hat{x}_i^h = \underbrace{x_i}_{\text{true frequency}} + \sum_{x_j \neq x_i} \underbrace{x_j 1_h(x_i, x_j)}_{\text{over-counting from hash collisions}}$$

Optimal Size

Error Bounds
per hash/array

$$\Pr [\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

Error Bounds
for the minimum

$$\hat{x}_i^h = x_i + \sum_{x_j \neq x_i} x_j 1_h(x_i, x_j)$$

hash collision
 $= \begin{cases} 1, & \text{if } h(x_i) = h(x_j) \\ 0, & \text{otherwise} \end{cases}$

Optimal Size

Error Bounds
per hash/array

$$\Pr[\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

Error Bounds
for the minimum

$$\hat{x}_i^h - x_i = \sum_{x_j \neq x_i} x_j 1_h(x_i, x_j)$$

estimation
error
over-counting
from hash collisions

Optimal Size

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We treat the **data as a constant** and the **hash as a random function** with certain properties.

Error Bounds
per hash/array

$$\Pr[\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

Error Bounds
for the minimum

$$\hat{x}_i^h - x_i = \sum_{x_j \neq x_i} x_j 1_h(x_i, x_j)$$

$$E[\hat{x}_i^h - x_i] = E\left[\sum_{x_j \neq x_i} \underbrace{x_j}_{\substack{\text{random} \\ \text{constant}}} 1_h(x_i, x_j)\right]$$

Optimal Size

Error Bounds
per hash/array

$$\Pr[\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

Error Bounds
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Optimal Size

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Error Bounds
per hash/array

$$\Pr[\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

Error Bounds
for the minimum

$$\hat{x}_i^h - x_i = \sum_{x_j \neq x_i} x_j 1_h(x_i, x_j)$$

$$E[\hat{x}_i^h - x_i] = \sum_{x_j \neq x_i} x_j E[1_h(x_i, x_j)]$$

Optimal Size

We treat the **data as a constant** and the **hash as a random function** with certain properties.

Error Bounds
per hash/array

$$\Pr[\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

$$\hat{x}_i^h - x_i = \sum_{x_j \neq x_i} x_j 1_h(x_i, x_j)$$

$$E[\hat{x}_i^h - x_i] = \sum_{x_j \neq x_i} x_j \underbrace{E[1_h(x_i, x_j)]}_{\leq \frac{1}{w}}$$

Error Bounds
for the minimum

Optimal Size

wikipedia.org/wiki/Universal_hashing

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We treat the **data as a constant** and the **hash as a random function** with certain properties.

Error Bounds
per hash/array

$$\Pr[\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

$$\hat{x}_i^h - x_i = \sum_{x_j \neq x_i} x_j 1_h(x_i, x_j)$$

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Error Bounds
for the minimum

Optimal Size

wikipedia.org/wiki/Universal_hashing

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Error Bounds
per hash/array

$$\Pr[\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

$$\hat{x}_i^h - x_i = \sum_{x_j \neq x_i} x_j 1_h(x_i, x_j)$$

$$E[\hat{x}_i^h - x_i] \leq \sum_{x_j \neq x_i} x_j \frac{1}{w} \leq \sum_{x_j} x_j \frac{1}{w}$$

Error Bounds
for the minimum

Optimal Size

Error Bounds
per hash/array

$$\Pr[\hat{x}_i^h - x_i \geq c \cdot E[\hat{x}_i^h - x_i]] \leq \frac{1}{c}$$

$$\hat{x}_i^h - x_i = \sum_{x_j \neq x_i} x_j 1_h(x_i, x_j)$$

$$E[\hat{x}_i^h - x_i] \leq \sum_{x_j \neq x_i} x_j \frac{1}{w} \leq \|\mathbf{x}\|_1 \frac{1}{w}$$

Error Bounds
for the minimum

Optimal Size

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Error Bounds
per hash/array

$$\Pr [\hat{x}_i^h - x_i \geq c \cdot \underbrace{E [\hat{x}_i^h - x_i]}_{\leq \frac{1}{w} \|\mathbf{x}\|_1}] \leq \frac{1}{c}$$

Error Bounds
for the minimum

Optimal Size

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Error Bounds
per hash/array

$$\Pr [\hat{x}_i^h - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1] \leq \frac{1}{c}$$

Error Bounds
for the minimum

Optimal Size

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Error Bounds
per hash/array

$$\Pr [\hat{x}_i^h - x_i \geq \underbrace{\varepsilon^h}_{\frac{c}{w}} \|\mathbf{x}\|_1] \leq \underbrace{\delta^h}_{\frac{1}{c}}$$

Error Bounds
for the minimum

Optimal Size

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Error Bounds
per hash/array

$$\Pr [\hat{x}_i^h - x_i \geq \underbrace{\varepsilon^h}_{\frac{c}{w}} \|\mathbf{x}\|_1] \leq \underbrace{\delta^h}_{\frac{1}{c}}$$

Error Bounds
for the minimum

Optimal Size

The **estimate for each hash** has
a well defined **L1 error bound**.

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Error Bounds
per hash/array

$$\Pr[\hat{x}_i^h - x_i \geq \underbrace{\varepsilon^h}_{\frac{c}{w}} \|\mathbf{x}\|_1] \leq \underbrace{\delta^h}_{\frac{1}{c}}$$

The **estimate for each hash** has
a well defined **L1 error bound**.

What about the minimum?

Optimal Size

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Error Bounds
per hash/array

$$\Pr[\hat{x}_i - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1] \leq ?$$

Error Bounds
for the minimum

Optimal Size

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Multiple hash functions work like **independent trials**.

Error Bounds
per hash/array

$$\Pr[\underbrace{\min_{h \in h_1 \dots h_d} \hat{x}_i^h}_{\hat{x}_i} - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1] \leq ?$$

Error Bounds
for the minimum

Optimal Size

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Error Bounds
per hash/array

$$\Pr[\underbrace{\min_{h \in h_1 \dots h_d} \hat{x}_i^h}_{\hat{x}_i} - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1] \leq ?$$

\Leftrightarrow

$$\prod_{h \in h_1 \dots h_d} \Pr[\hat{x}_i^h - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1] \leq ?$$

Error Bounds
for the minimum

Optimal Size

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Error Bounds
per hash/array

Error Bounds
for the minimum

Optimal Size

$$Pr \left[\underbrace{\min_{h \in h_1 \dots h_d} \hat{x}_i^h}_{\hat{x}_i} - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1 \right] \leq ?$$

$$\Leftrightarrow$$

$$\prod_{h \in h_1 \dots h_d} \underbrace{Pr \left[\hat{x}_i^h - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1 \right]}_{\leq \frac{1}{c}} \leq ?$$

error bound per hash

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Error Bounds
per hash/array

Error Bounds
for the minimum

Optimal Size

$$Pr \left[\underbrace{\min_{h \in h_1 \dots h_d} \hat{x}_i^h}_{\hat{x}_i} - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1 \right] \leq ?$$

$$\Leftrightarrow$$

$$\prod_{h \in h_1 \dots h_d} \underbrace{Pr \left[\hat{x}_i^h - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1 \right]}_{\leq \frac{1}{c}} \leq \frac{1}{c^d}$$

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Error Bounds
per hash/array

Error Bounds
for the minimum

Optimal Size

$$Pr \left[\underbrace{\min_{h \in h_1 \dots h_d} \hat{x}_i^h}_{\hat{x}_i} - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1 \right] \leq \frac{1}{c^d}$$

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Error Bounds
per hash/array

Error Bounds
for the minimum

Optimal Size

$$Pr \left[\hat{x}_i - x_i \geq \frac{c}{w} \|\mathbf{x}\|_1 \right] \leq \frac{1}{c^d}$$

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Error Bounds
per hash/array

Error Bounds
for the minimum

Optimal Size

$$Pr \left[\hat{x}_i - x_i \geq \underbrace{\varepsilon}_{\frac{c}{w}} \mid \|\mathbf{x}\|_1 \leq \underbrace{\delta}_{\frac{1}{c^d}} \right]$$

*We have proven the error bounds!
But what about the constant c ?*

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Choosing $c=e$ **minimizes** the
total **number of counters**.

Error Bounds
per hash/array

Error Bounds
for the minimum

Optimal Size

$$\varepsilon = \frac{e}{w} \Rightarrow w = \left\lceil \frac{e}{\varepsilon} \right\rceil \quad (\text{hash range})$$

$$\delta = \frac{1}{e^d} \Rightarrow d = \left\lceil \ln \frac{1}{\delta} \right\rceil \quad (\text{\#hashes})$$

$$d \cdot w = \frac{c}{\varepsilon} \log_c \frac{1}{\delta} \stackrel{\text{minimize}}{=} \frac{e}{\varepsilon} \ln \frac{1}{\delta}$$

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For **every** \mathbf{c} , there is a pair (d, w) achieving
the error bound and confidence (ε, δ) .

Error Bounds
per hash/array

Error Bounds
for the minimum

Optimal Size

$$\varepsilon = \frac{c}{w} \Rightarrow w = \left\lceil \frac{c}{\varepsilon} \right\rceil \quad (\text{hash range})$$

$$\delta = \frac{1}{c^d} \Rightarrow d = \left\lceil \log_c \frac{1}{\delta} \right\rceil \quad (\text{\#hashes})$$

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A **CountMin** sketch recipe

Given ε, δ , **choosing**

Error Bounds
per hash/array

Error Bounds
for the minimum

Optimal Size

$$w = \left\lceil \frac{e}{\varepsilon} \right\rceil \quad (\text{hash range})$$

$$d = \left\lceil \ln \frac{1}{\delta} \right\rceil \quad (\text{\#hashes})$$

requires the **minimum number of counters** s.t. the CountMin Sketch
can guarantee that

$$\hat{x}_i - x_i \geq \varepsilon \|\mathbf{x}\|_1$$

with a probability less than δ

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A **CountMin sketch** uses the same principles as a counting bloom filter, but is **designed** to have **provable L1 error bounds** for frequency queries.

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A **CountMin sketch** uses the same principles as a counting bloom filter, but is **designed** to have **provable L1 error bounds** for frequency queries.

→ only one design out of many!

67

A **CountMin sketch** uses the same principles as a counting bloom filter, but is **designed** to have **provable L1 error bounds** for frequency queries.

66

CountMin sketch recipe

Choose $d = \left\lceil \ln \frac{1}{\delta} \right\rceil$, $w = \left\lceil \frac{e}{\epsilon} \right\rceil$

Then $\hat{x}_i - x_i \geq \epsilon \|\mathbf{x}\|_1$ with a probability less than δ

A **Count sketch** uses the same principles as a counting bloom filter, but is **designed** to have **provable L2 error bounds** for frequency queries.

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The Count sketch uses **additional hashing** to give **L2 error bounds**, but requires more **resources**.

```
CountMin sketch
h1, ..., hd: U → {1, ..., w}

COUNT xi:
for h in h1, ..., hd:
  Regh[h(xi)] + 1

QUERY xi:
return minh in h1, ..., hd(
  Regh[h(xi)]
)
```

The Count sketch uses **additional hashing** to give **L2 error bounds**, but requires more **resources**.

```
CountMin sketch
h1, ..., hd: U → {1, ..., w}

COUNT xi:
for h in h1, ..., hd:
  Regh[h(xi)] + 1

QUERY xi:
return minh in h1, ..., hd(
  Regh[h(xi)]
)
```

```
Count sketch
h1, ..., hd: U → {1, ..., w}
g: U → {+1, -1}

COUNT xi:
for h in h1, ..., hd:
  Regh[h(xi)] + g(xi)

QUERY xi:
return medianh in h1, ..., hd(
  Regh[h(xi)] * g(xi)
)
```

The Count sketch uses **additional hashing** to give **L2 error bounds**, but requires more **resources**.

The Count sketch uses **additional hashing** to give **L2 error bounds**, but requires more **resources**.

```
CountMin sketch recipe

Choose d = ⌈ln 1/δ⌉, w = ⌈e/ε⌉

Then x̂i - xi ≥ ε ||x||1 with a probability less than δ
```

```
CountMin sketch recipe

Choose d = ⌈ln 1/δ⌉, w = ⌈e/ε⌉

Then x̂i - xi ≥ ε ||x||1 with a probability less than δ
```

```
Count sketch recipe

Choose d = ⌈ln 1/δ⌉, w = ⌈e/ε2⌉

Then x̂i - xi ≥ ε ||x||2 with a probability less than δ
```

Sketches are the new black

OpenSketch
NSDI '13

[source]



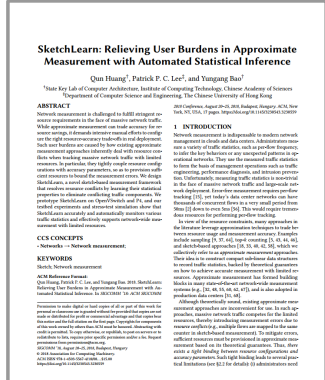
UnivMon
SIGCOMM '16

[source]



SketchLearn
SIGCOMM '18

[source]



Sketches are the new black

OpenSketch
NSDI '13

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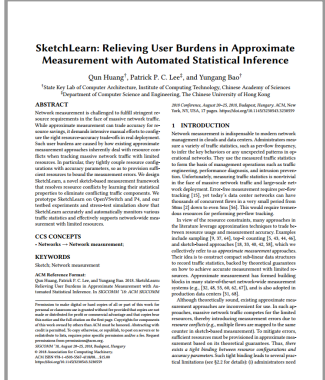
UnivMon
SIGCOMM '16

[source]



SketchLearn
SIGCOMM '18

[source]



SketchLearn combines multiple sketches with elaborate post-processing for flexibility

SketchLearn: Relieving User Burdens in Approximate Measurement with Automated Statistical Inference

Qun Huang[†], Patrick P. C. Lee[‡], and Yungang Bao[‡]
[†]State Key Lab of Computer Architecture, Institute of Computing Technology, Chinese Academy of Sciences
[‡]Department of Computer Science and Engineering, The Chinese University of Hong Kong

ABSTRACT
Network measurement is challenged to fulfill stringent resource requirements in the face of massive network traffic. While approximate measurement can trade accuracy for resource savings, it demands intensive manual efforts to configure the right resource-accuracy trade-offs in real deployment. Such user burdens are caused by how existing approximate measurement approaches inherently deal with resource conflicts when tracking massive network traffic with limited resources. In particular, they tightly couple resource configurations with accuracy parameters, so as to provision sufficient resources to bound the measurement errors. We design SketchLearn, a novel sketch-based measurement framework that resolves resource conflicts by learning their statistical properties to eliminate conflicting traffic components. We prototype SketchLearn on OpenVSwitch and P4, and our testbed experiments and stress-test simulation show that SketchLearn accurately and automatically monitors various traffic statistics and effectively supports network-wide measurement with limited resources.

CCS CONCEPTS
• Networks → Network measurement;
KEYWORDS
Sketch; Network measurement

ACM Reference Format:
Qun Huang, Patrick P. C. Lee, and Yungang Bao. 2018. SketchLearn: Relieving User Burdens in Approximate Measurement with Au-

2018 Conference, August 20–25, 2018, Budapest, Hungary. ACM, New York, NY, USA, 17 pages. <https://doi.org/10.1145/3230543.3230559>

1 INTRODUCTION
Network measurement is indispensable to modern network management in clouds and data centers. Administrators measure a variety of traffic statistics, such as per-flow frequency, to infer the key behaviors or any unexpected patterns in operational networks. They use the measured traffic statistics to form the basis of management operations such as traffic engineering, performance diagnosis, and intrusion prevention. Unfortunately, measuring traffic statistics is non-trivial in the face of massive network traffic and large-scale network deployment. Error-free measurement requires per-flow tracking [15], yet today’s data center networks can have thousands of concurrent flows in a very small period from 50ms [2] down to even 5ms [56]. This would require tremendous resources for performing per-flow tracking.

In view of the resource constraints, many approaches in the literature leverage approximation techniques to trade between resource usage and measurement accuracy. Examples include sampling [9, 37, 64], top-*k* counting [5, 43, 44, 46], and sketch-based approaches [18, 33, 40, 42, 58], which we collectively refer to as *approximate measurement* approaches. Their idea is to construct compact sub-linear data structures to record traffic statistics, backed by theoretical guarantees on how to achieve accurate measurement with limited resources. Approximate measurement has formed building blocks in many state-of-the-art network-wide measurement

...and many more!

Today we’ll talk about: important questions, how ‘sketches’ answer them, limitations of ‘sketches’, and my master thesis :)

Sketches **compute statistical summaries**,
favoring elements with **high frequency**.

$$Pr \left[\underbrace{\hat{x}_i - x_i}_{\text{estimation error}} \geq \varepsilon \underbrace{\|\mathbf{x}\|_1}_{\text{relative to sum of all elements}} \right] \leq \delta$$

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Sketches **compute statistical summaries**,
favoring elements with **high frequency**.

$$\text{Let } \varepsilon = 0.01, \|\mathbf{x}\|_1 = 10000 \quad (\Rightarrow \varepsilon \cdot \|\mathbf{x}\|_1 = 100)$$

Assume two flows x_a, x_b ,

$$\text{with } \|x_a\|_1 = 1000, \|x_b\|_1 = 50$$

Error relative to **stream size**: 1%

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|
|
high frequency
low frequency

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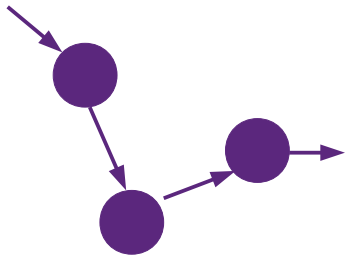
Error relative to **stream size**: 1%

flow size: x_a : 10%, x_b : **200%**

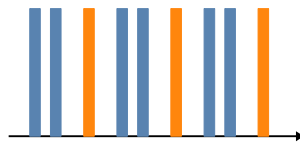
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Other Problems a Sketch **can't handle**

causality



patterns



rare things

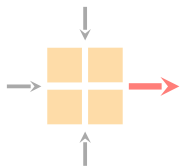


Regardless of their limitations, sketches provide **trade-offs between resources and error**, and **provable guarantees** to rely on.

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Advanced Topics in Communication Networks
Programming Network Data Planes



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